

## FORMULAS OVER MINIMAL STRUCTURES

Baissalov Y.<sup>1</sup>, Tussupov J.<sup>2</sup>

Astana IT University<sup>1</sup> and L.N. Gumilyov Eurasian National University<sup>2</sup>, Nur-Sultan, Kazakhstan

E-mail: [yerzhan.baissalov@astanait.edu.kz](mailto:yerzhan.baissalov@astanait.edu.kz) and [tussupov@mail.ru](mailto:tussupov@mail.ru)

We present one purely syntactic result on the structure of formulas over a minimal non-ordered structure (in the sense of [1]) with the definable generic type. Let  $M$  be such a structure.

**Definition 1.** Let  $\varphi(x; \bar{y})$  be a formula over  $M$  with free variables  $y = (y_1, y_2, \dots, y_n)$  and  $x$ . We say the variable  $x$  is tame if the set  $\varphi(M; \bar{b})$  is finite for any  $\bar{b} \in M$ .

**Definition 2.** A formula over  $M$  is called tame if every free variable in it is tame.

**Theorem.** Each formula over  $M$  is equivalent to a Boolean combination of tame formulas.

### References

1. K. Krupiński, P. Tanović and F. O. Wagner, Around Podewski's conjecture, arXiv:1201.5709v2.

## SOME PROPERTIES OF COUNTABLE MODELS OF SMALL ORDERED THEORIES

Baizhanov B.S.

*Институт математики и математического моделирования, Алматы, Казахстан*

The report is devoted to the properties of countable models of small theories. A theorem is proved (together with T. Zambarnaya) on the existence of models over a countable set. All built models have the same finite diagram. In addition, the report considers conditions on 1-types of small ordered theories in terms of 2-formulas acting on the set of realizations of 1-type that provide the maximum number of countable models.

## PERMUTATION GROUPS OF FINITE MORLEY RANK

Alexandre V. Borovik

*University of Manchester, Manchester, United Kingdom*

Binding groups are model-theoretic analogues of Galois groups; they were introduced in the 1970s by Zilber. They are very natural mathematical objects; to explain that we need a few words about permutation groups.

Given a permutation group  $G$  on a set  $X$ , a subset of  $X$  is said to be a base for  $G$  if its pointwise stabilizer in  $G$  is trivial. The minimal size of a base for  $G$  is denoted by  $b(G)$ . Finite bases, if exist, yield parameterizations, in terms of  $X$ , and structural analysis of group actions: if  $b_1, \dots, b_n$  is a base, each permutation  $g \in G$  is uniquely determined by an  $n$ -tuple  $(b_1^g, \dots, b_n^g) \in X^n$ .

Now let  $X$  be a finite dimensional vector space and  $G$  its automorphism group. A basis of  $X$  as a vector space is also a base for the action of  $G$ , and elements of  $G$  can be encoded as images of this base, that is, finite tuples of vectors, commonly known as matrices; the dependencies between vectors in the space allow us to express composition of automorphisms as product of matrices: the group  $G$  becomes definable in  $X$ . It was Zilber's seminal discovery that a similar construction can