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## NUMERICAL MODELING OF THE PROCESS OF EXTRUSION OF HIGH-VISCOSITY PASTES

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**Abstract.** This paper provides a theoretical consideration of the process of paste extrusion using a piston dispenser. The paste is considered as a highly viscous suspension of terpineol and silver particle powder. As a result of numerical modeling, the distribution of silver particles in a steady paste flow was obtained. The excess pressure in the piston depending on its speed and the effective width of the track depending on the piston speed were obtained. Modeling showed that the viscosity of the paste has the greatest influence on the extrusion process. Application of the obtained dependencies will allow you to control the paste extrusion process.

**Keywords:** extrusion, piston dispenser, silver paste, viscosity, terpineol.

### 1. Introduction

The application of additive printing technology allowing manufacturing hybrid integrated circuits and devices is gaining popularity due to the reduction in the time expenditures on prototyping and obtaining finished products [1-3]. Studies are being conducted in the field of inkjet printing; however, using this technology allows forming only thin-film elements up to 1  $\mu\text{m}$  thick. The inkjet printing technology demonstrates the examples of studying the production of RFID tags [4-7], antennas [8-12] of different types: meander, dual-band, monopole, dipole, ultra-wideband, etc.

Printers that are based on piston, screw and pneumatic extrusion of pastes are used to obtain thick-film elements [1]. The composition and characteristics of the pastes intended for piston and screw extrusion differ significantly from the inks used for inkjet printing, as well as from the pastes used for screen printing. The main difference consists in the concentration of solid particles and the material viscosity [2].

The works [13-15] describe the application of piston extrusion of the material used to print microwave antenna systems. The considered antenna systems operate in the range from 2.5 GHz up to 4.7 GHz. The frequency losses of the printed antennas are 5.3 dB at a frequency of 2.5 GHz. The geometric dimensions of the printed antennas are no more than 20×20 mm. A technique used for extracting the frequency electrical parameters of conductive pastes, on the basis of which microstrip lines were formed by piston extrusion, is described in [16]. A thickness increase in the microstrip line led to a decrease in the frequency losses from 12 dB to 6 dB at a frequency of 1 GHz. A printed multilayer conformal X-band antenna array is considered in [17]. The antenna represents a 32-element X-band superimposed matrix and is manufactured on a surface having several curvilinear lines. The peak antenna gain exceeds 15 dB at a frequency of 10.4 GHz.

Printing the planar components such as inductor, resistor, capacitor is presented in [18,19]. The printed inductor consists of 25 turns. The geometric dimensions of the printed inductor are 14×14 mm while the line width is 100  $\mu\text{m}$  and the distance between the lines is about 75  $\mu\text{m}$ . The measured electrical parameters of the inductor have an inductance of 5.42  $\mu\text{H}$ , a resistance of 12.7 k $\Omega$  and a capacitance of 50 pF.

Depending on the number of the printed resistor layers, the resistance of the active region varies from 25 Ohms to 650 Ohms. The printed capacitor has a capacity of 322 pF at 1 kHz and a breakdown voltage of 1000 V.

During piston extrusion [3,20], a piston is used to extrude the material being inside the syringe. The extruded volume and the flowrate of the pastes depend on the piston displacement inside the syringe. The volume of the extruded pastes and the extrusion rating are related to the piston movement speed [21]. The application of the pastes having different viscosities depends on the power of the drive motor and the mechanical system.

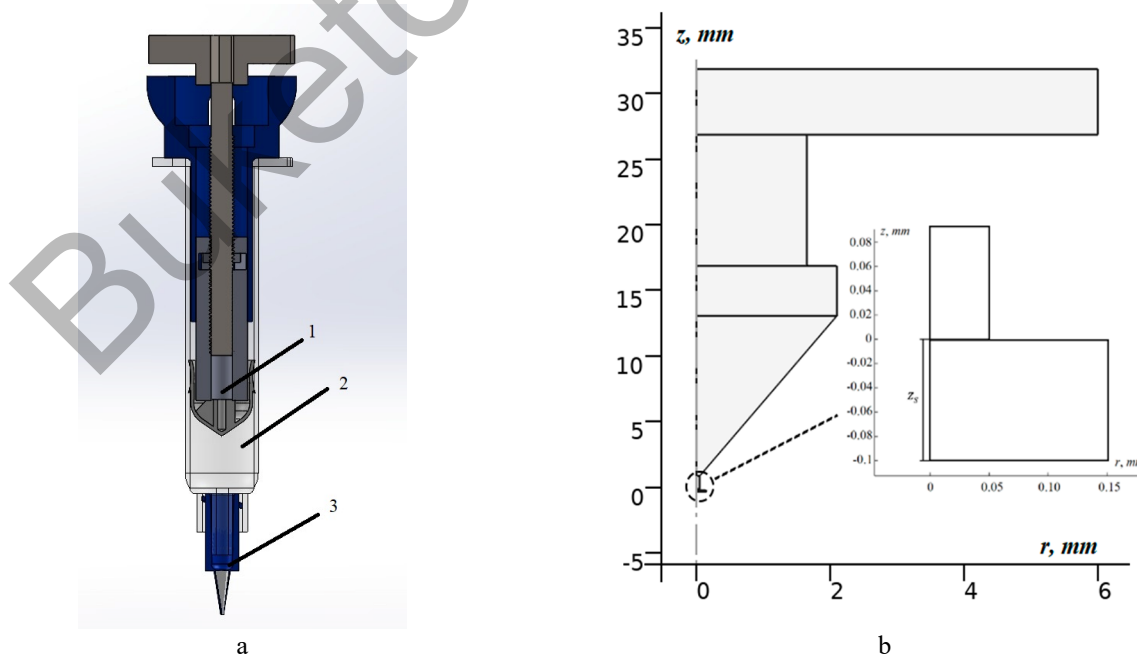
The formation of the printed films structure requires understanding the process of forming a uniform, continuous flow of the paste, its exit from the nozzle and distribution over the substrate. The pressure created in the syringe, the dispenser movement speed and the distance between the nozzle and the substrate influence the printed films quality. The paste extrusion rating depends on such rheological characteristics as viscosity, density, wetting, etc. [22]. Ambient temperature or high pulses of pressure, which can change the outflow rate during the extrusion process, can influence the paste viscosity change.

The dispenser movement rate must be consistent with the linear velocity of the out-flow of the pastes from the nozzle [23]. An extremely high flow rate, as compared to the movement rate of the dispenser, will lead to excessive deformations of the formed films and even to film disruptions [21]. Therefore, the relationship between the movement rate of the dispenser and the linear velocity of the extruded flow, which is a function of a complex extrusion process, is crucial for successful deposition and creation of the desired films.

Obtaining high-quality prototypes of printed circuit boards by means of the paste extrusion requires investigating different modes of the printing system operation. This work is devoted to the theoretical study of the capabilities of the dispenser operation during piston extrusion of the paste, consisting of an organic binder (terpineol) and a powder (silver particles).

## 2. Materials and methods

Let us consider the problem of numerical simulation of squeezing a paste consisting of silver and terpineol particles through a nozzle into the air. Extrusion is carried out in a gravity field using a piston dispenser. (Fig. 1a). This dispenser has axial symmetry, so numerical modeling was carried out in a cylindrical coordinate system. Figure 1b shows the calculated area of the inner part of the dispenser and the air ( $z_s$  area).



**Fig 1.** The computational region corresponding to this dispenser (a) 1 is piston, 2 is syringe, 3 is nozzle. Computational region of the model corresponding to the area filled with the paste and air (b).

The left boundary of the calculation area is the axis of symmetry. All other boundaries, with the exception of the top and bottom ones, are considered as impenetrable walls. At the initial moment of time, the dispenser is filled with paste, which is squeezed out under the action of a piston moving at a constant speed along the  $z$  axis, i.e. a constant paste speed is set perpendicular to the upper boundary. The lower part of the  $z_s$  area is an open boundary that air and paste can leave. The pressure at the lower boundary is equal to atmospheric pressure. In this case, for a correct description of the extrusion of paste with silver particles, three-phase medium air/terpineol/silver particles can be considered. Obviously, the case of contact of silver particles with air is not relevant for our task, therefore we will limit ourselves to a description in which only contacts between silver particles with terpineol and terpineol with air are assumed. There are also impermeable walls (syringe surface) where the air/paste/syringe surface area is present.

Let's consider a standard approach to describe our problem based on solving a system of the following equations:

$$\rho \frac{\partial \vec{v}}{\partial t} + \rho(\vec{v} \cdot \nabla)\vec{v} = \nabla \cdot (-p\mathbf{I} + \mathbf{K}) + \rho\vec{g} + \vec{F}_\sigma + \vec{F}_\theta \quad (1)$$

$$\frac{\partial \rho}{\partial t} + \nabla \rho \vec{v} = 0 \quad (2)$$

$$\frac{\partial \phi}{\partial t} + \vec{v} \nabla \phi = \zeta \nabla \cdot \left( \varepsilon \nabla \phi - \phi(1-\phi) \frac{\nabla \phi}{|\nabla \phi|} \right) = 0 \quad (3)$$

$$\frac{3}{4} \frac{C_d}{d_d} \rho_c |\vec{v}_{slip}| \vec{v}_{slip} = \frac{\rho_2 - \rho_d}{\rho_2} \left( \rho_2 \frac{\partial \vec{v}}{\partial t} + \rho_2 (\vec{v} \cdot \nabla)\vec{v} - \rho_2 \vec{g} \right) \quad (4)$$

where Eq. (1) is the Navier-Stokes equation, where  $\Delta$  is the Laplace operator,  $\rho$  is the density,  $p$  is the pressure,  $\vec{v} = (v^1, v^2)$  is the velocity vector field,  $\vec{F}_\sigma$  is the volume force corresponding to surface tension, which characterizes the behavior of the paste at the paste-air interface. This force can be represented in the following form:

$$\vec{F}_\sigma = \sigma \delta \kappa \vec{n},$$

where  $\sigma$  is the terpineol-air surface tension coefficient,  $\delta = 6|\nabla \phi| \cdot |\phi(1-\phi)|$  is a smooth approximation of the Dirac delta function,  $\kappa$  is the curvature,  $\vec{n}$  is the unit vector of the normal to the interface of the terpineol-air phases,  $\mathbf{I}$  is the identity matrix,  $\mathbf{K}$  is the viscous stress tensor,  $\vec{g}$  is the acceleration of gravity. A force arises at the air/paste/syringe surface boundary  $\vec{F}_\theta$ , directed normal to the paste-air surface:

$$\vec{F}_\theta = \sigma \delta (\vec{n}_{wall} \cdot \vec{n} - \cos(\theta)) \vec{n},$$

where  $\vec{n}_{wall}$  is the unit vector of the normal to the surface of the syringe.

The viscous stress tensor in the case of a compressible fluid has the form:

$$\mathbf{K} = \mu(\nabla \vec{v} + (\nabla \vec{v})^T) - \frac{2}{3} \mu(\nabla \cdot \vec{v})\mathbf{I},$$

where  $\nabla \vec{v}$  is the velocity gradient (second-order tensor),  $( )^T$  indicates the transposition,  $\mu$  is the dynamic viscosity coefficient.

The air from the paste differs significantly in density and viscosity, therefore, in expressions (1) and (5), the viscosity and density are written as:

$$\rho = \rho_1 + (\rho_2 - \rho_1)\phi,$$

$$\mu = \mu_1 + (\mu_2 - \mu_1)\phi,$$

where  $\rho_1$ ,  $\mu_1$  are the density and viscosity of the air,  $\rho_2$ ,  $\mu_2$  are the density and viscosity of the paste,  $\phi$  is a level function obeying equation (3), which is zero in the paste area and one in the air [24], where the  $\zeta$  parameter characterizes the maximum speed and the  $\varepsilon$  parameter defines the phase boundary thickness.

The paste velocity  $\vec{v}$  depends on the organic binder velocity  $\vec{v}_c$  and the relative velocity of the dispersed phase particles  $\vec{v}_{slip}$  as follows:

$$\vec{v} = \frac{s_c \rho_c \vec{v}_c + s_d \rho_d (\vec{v}_c + \vec{v}_{slip})}{\rho_2} \quad (5)$$

where  $\rho_2 = s_c \rho_c + s_d \rho_d$ ,  $s_d$  takes values from 0 to 1 and characterizes the volume fraction of the dispersed phase particles and  $s_c = 1 - s_d$ .

Note that at the initial moment of time, silver particles are surrounded by terpeneol, and contact between silver is undesirable, therefore, numerical modeling considered only those solutions in which there was no contact between silver particles and air. In this case, the velocity  $\vec{v}$  is the velocity of the paste where it is present and the velocity of the air where the paste is absent. The velocity field obeys the corresponding continuity equation Eq. (2). The Eq. (4) describes the behavior of solid particles in a liquid, where  $C_d$  is the coefficient characterizing the balance between viscous resistance and buoyancy forces influencing the dispersed phase,  $d_d$  is the effective diameter of the dispersed phase particles (solid particles),  $\rho_d$  is the dispersed phase density,  $\vec{v}_{slip}$  is the velocity of the dispersed phase particles relatively the organic binder,  $\rho_c$  is the organic binder density.

A number of approximations of the Rayleigh curve are proposed to describe the transition region for the Reynolds numbers  $Re = \frac{d_d \rho_c |\vec{v}_{slip}|}{\mu_2}$  that are less than 1000 [25]. The smallest relative error of up to 3 % in the transition region is shown by the Schiller-Neumann approximation [26], according to which the coefficient  $C_d$  in the Eq. (4) has the following form:

$$C_d = \frac{24}{Re} (1 + 0.15 Re^{0.687})$$

Numerical simulation of the system (1)-(4) was carried out under the following initial and boundary conditions:

1. At the initial moment of time (Figure 2a), the dispenser is completely filled with paste ( $\phi = 1$ ), and the extrusion area is air ( $\phi = 0$ ), while the velocity field is zero.
2. As noted above, at the lower boundary of the free space corresponding to the air, the pressure is equal to atmospheric, at the upper boundary a constant value of the paste feed rate  $v_{in} = const$  (normal) is set, which corresponds to a constant piston speed. All other boundaries (except for the axis of symmetry) the boundary conditions of an impermeable wall correspond, which is written as follows:

$$\vec{v} \cdot \vec{n} = 0,$$

$$\vec{n} \cdot \left( \varepsilon \nabla \phi - \phi(1 - \phi) \frac{\nabla \phi}{|\nabla \phi|} \right) = 0.$$

Let us note that the main geometric characteristics of the internal area of the dispenser are a nozzle diameter of 0.1 mm and a piston diameter of 12 mm.

The paste extrusion was modeled using the COMSOL Multiphysics 6.1 package. In this study, the physical modules Laminar Flow, Level Set and Phase Transport, as well as the calculation modules Phase Initialization and Time-Dependent, were used. An approach that is similar to the one applied in the work was used [26]. The problem was solved using the finite element method, while an appropriate partition was selected for each of the regions, and a finite element grid was selected for each region taking into account the proportion of silver particles in the paste  $s_d$  (Fig. 2b).

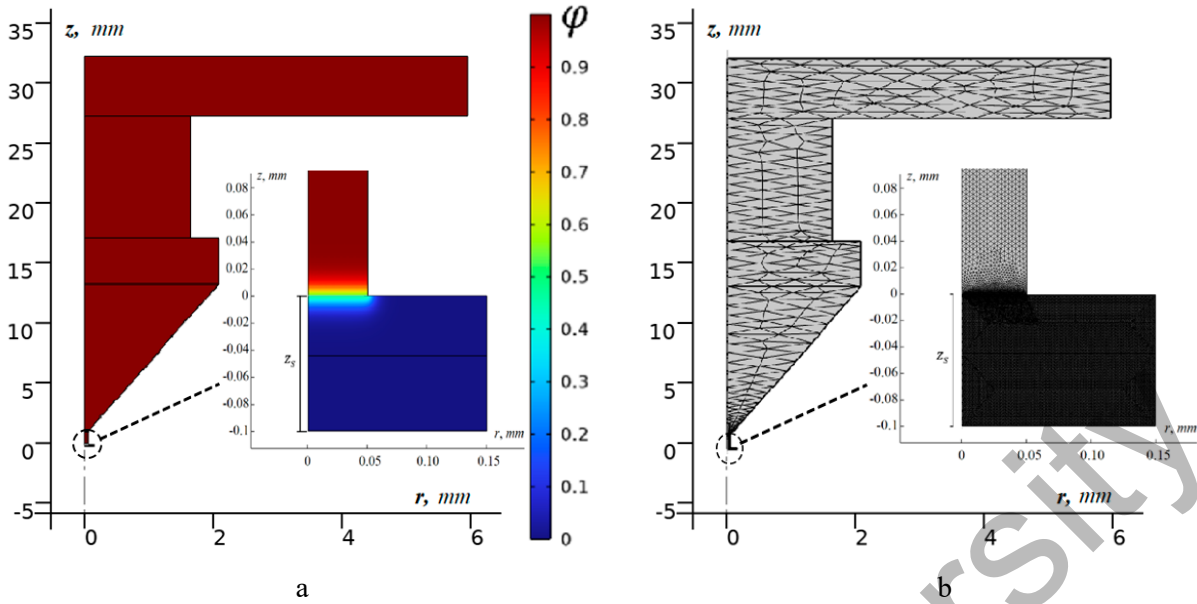


Fig. 2 Initial paste distribution in the calculation area (a) and the grid used for calculation (b)

The (1)-(4) system was numerically modeled using the parameters given in Table 1, considering the influence of surface tension and gravity forces. Table 1 provides the initial physical parameters.

Table 1. Initial parameters for modeling

Parameter	Value	Reference
Terpineol density $\rho_c$	930 kg/m <sup>3</sup>	[27]
Silver density $\rho_d$	10500 kg/m <sup>3</sup>	[28]
Air density $\rho_1$	1.28 kg/m <sup>3</sup>	[29]
Sliver particle size $d_d$	2 · 10 <sup>-6</sup> m	[30]
Terpineol dynamic viscosity $\mu_c$	0.097 Pa · s	[27]
Air dynamic viscosity $\mu_1$	1.81 · 10 <sup>-5</sup> Pa · s	[29]
Terpineol surface tension	0.033 N/m	[27]
Wetting angle at the interface of terpineol/air/syringe surface	$\pi/2$	[31]

The dynamic viscosity coefficient  $\mu$  of the paste is of particular interest since it significantly depends on the shear rate  $\dot{\gamma}$  in the local region of the space (Fig. 2). This dependence is well described by the Carreau's model [26]:

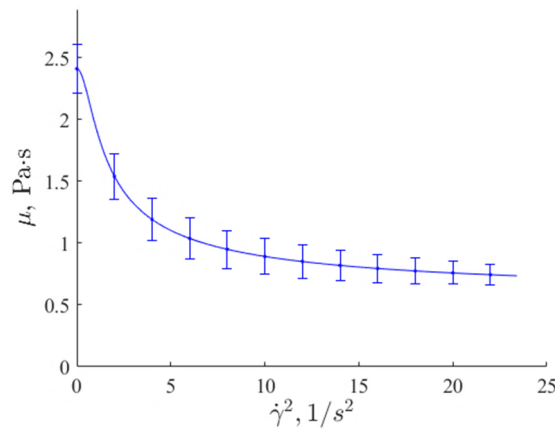
$$\mu_2 = \mu_{inf} + (\mu_0 - \mu_{inf})(1 + (\lambda\dot{\gamma})^2)^{(n-1)/2} \quad (6)$$

In this case  $\mu_{inf}$ ,  $\mu_0$ ,  $\lambda$ ,  $n$  are the Carreau's model parameters determined by the experimental data approximation.

A rotary viscometer ViscoQC 300 (Anton Paar, Austria, Graz) in the Heli-Plus configuration was used to determine the dynamic viscosity of the paste; this viscometer allowed obtaining the dependence of the paste dynamic viscosity on the shear rate. The approximation of this dependence in accordance with the Carreau's model Eq. (11) is shown in Fig. 3.

Note that the experimentally obtained dependence (Fig. 3), approximated using the model (6), allows in the process of modeling the extrusion of paste to calculate the viscosity depending on the shear rate  $\dot{\gamma}$ , which is affected by the redistribution of particles during the movement of the paste.

The following parameters correspond to the dependence presented in Fig. 3:  $\mu_{inf} = 0.053$  MPa,  $\mu_0 = 0.241$  MPa,  $\lambda = 1.151$  s,  $n = 0.324$ .



**Fig. 3.** Approximation of the experimentally obtained dependence of the viscosity on the squared shear velocity with the Carreau’s model Eq. (6)

In the Eq. (5), the concept of the volume fraction of the dispersed phase (silver powder) is used, but in experiments, the paste is usually prepared by the mass fraction of the silver powder:

$$\omega = \frac{m_d}{m_d + m_c} \tag{7}$$

where  $m_d$ ,  $m_c$  are the masses of the silver powder and terpeneol, respectively.

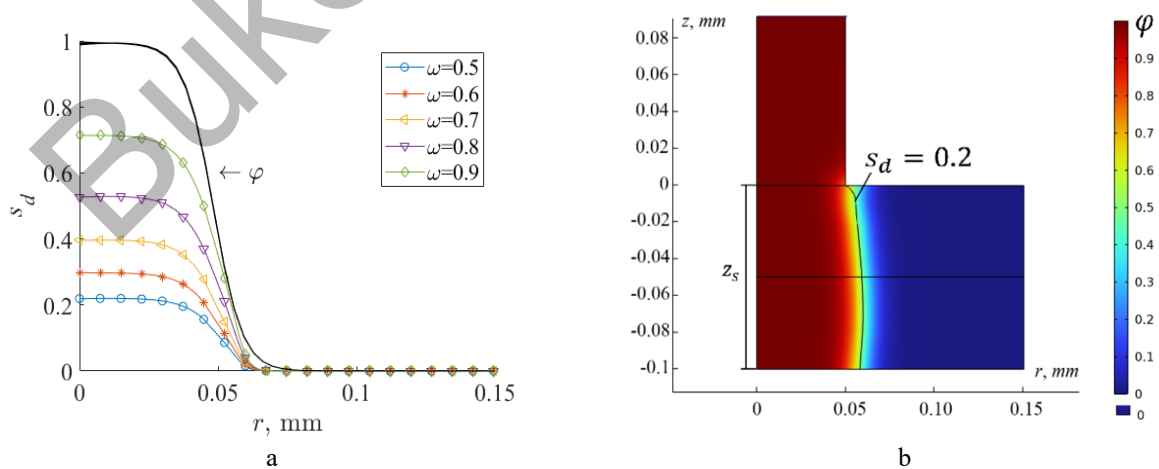
Knowing the mass fraction of the silver powder allows calculating its volume fraction as follows:

$$s_d = \frac{\rho_c \omega}{\rho_c \omega + \rho_d (1 - \omega)} \tag{8}$$

where  $\rho_d$ ,  $\rho_c$  are the density of the silver powder and terpeneol, respectively.

### 3. Results and discussion

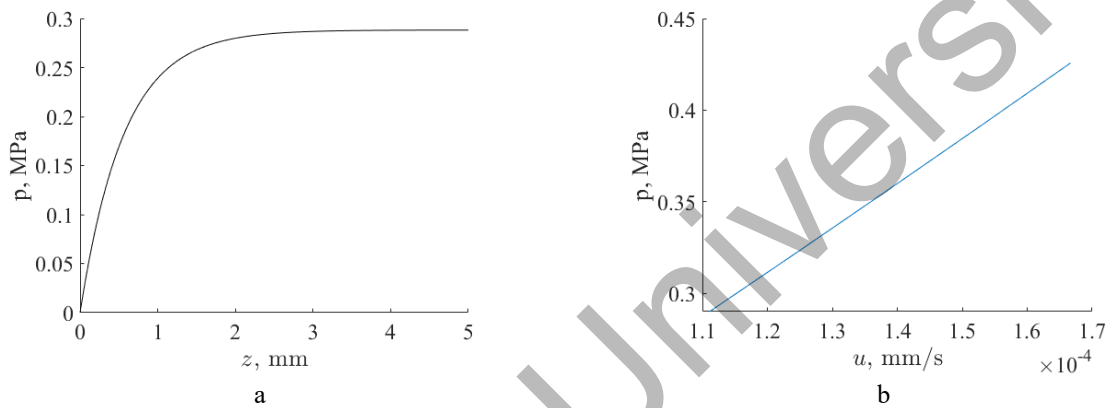
The Eq. (1)-(4) system was numerically modeled for different values of the mass fraction of the silver powder Eq. (7) and the piston velocity. Fig. 4a shows the dependences of the volume fraction of the silver powder and the dependence of the function  $\varphi$  on the distance  $r$  up to the vertical axis of the dispenser in the steady-state extrusion mode at a distance of  $z_s = 0.1$  mm (Fig. 4b) from the outlet section of the nozzle, obtained by means of the numerical modeling. Fig. 4b demonstrates the distribution of the function  $\varphi$  in the computational region of the nozzle and below the nozzle when the mass fraction is  $\omega = 0.7$ .



**Fig. 4.** Dependences of the volume fraction of the silver powder and the dependence of the function  $\varphi$  on the distance  $r$  up to the vertical axis of the dispenser in the steady-state extrusion mode at a distance of  $z_s = 0.1$  mm from the outlet section of the nozzle (a), distribution of the function  $\varphi$  in the computational region of the nozzle and below the nozzle when the mass fraction is  $\omega = 0.7$ ; an additional line of the volume fraction level has been drawn ( $s_d = 0.02$ ) (b).

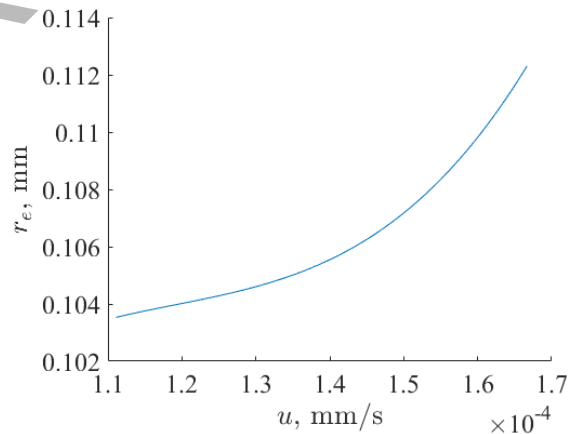
The function  $\varphi$  type practically does not depend on the mass fraction of the silver powder present in the paste; however, the volume fraction distribution of the silver powder varies significantly. At a sufficiently large interval, when the distance  $r$  is increasing, the volume fraction of the dispersed phase remains constant, but it decreases nonlinearly closer to the edge. An increase in the mass fraction of the silver powder obviously leads to a significant increase in the cross-sectional area of the printed tracks, which is proportional to the area under the curves  $s_d$  shown in Fig. 3b (the effective width of the track at  $\omega=0.7$  is  $r_e=0.122$  mm). The calculations have shown that this dependence is nonlinear, but it is linear in the case of using the volume fraction instead of the mass fraction, which is related to the mass fraction according to the Eq. (8). Let us note that in practice the proposed statements are valid for a stable (debugged) technical process.

Let us consider the dependence of the overpressure (pressure above atmospheric) present on the vertical axis of the dispenser on the distance up to the nozzle section at the outlet as a characteristic of a stable process (Fig. 5a). The maximum pressure inside the dispenser was 0.288 MPa. Changing the piston speed allows obtaining a maximum overpressure that depends on the speed (Fig. 5b).



**Fig. 5.** Dependence of the overpressure present on the vertical axis of the dispenser (the mass fraction is  $\omega=0.7$ ) on the distance to the nozzle section at the outlet (a) and the dependence of the maximum overpressure present in the piston on its velocity (b).

A linear increase in the overpressure accompanied by a piston speed increase leads to a critical value at which the piston will not start to deform; but before reaching this value, the stable operation of the technological process is disrupted because the piston speed increase entails a non-linear increase in the effective width of the track  $r_e$  (Fig. 6).



**Fig. 6.** Dependence of the effective width of the track  $r_e$  on the piston speed when  $\omega=0.7$ .

Fig. 6 shows that the nonlinear growth of the effective width of the track begins at a speed exceeding the value of  $1.3 \cdot 10^{-4}$  mm/s. The calculations were additionally carried out in the case of different surface tensions and wetting angles, which proved that the wetting angle did not influence significantly the extrusion process, and the surface tension increase, when other parameters were fixed, led to a strong nonlinearity depending on  $r_e(u)$ . That is, it is necessary to monitor the terpeneol quality when preparing the paste.

According to the numerical modeling results, the effective parameters of the printing system operation are the following. The distance of the dispenser from the substrate is  $z_s = 0.1$  mm, the mass fraction of the silver powder in the paste is  $\omega = 0.7$ , the piston speed is  $1.1 \cdot 10^{-4}$  mm/s, the maximum pressure in the dispenser is 0.288 MPa, the effective width of the track is  $r_e = 0.122$  mm.

#### 4. Conclusions

In this work, a numerical simulation of the piston extrusion process was carried out using the example of terpeneol paste and silver particle powder. The main emphasis is placed on obtaining the dependencies for the basic physical quantities on the control parameters and properties of the paste that characterize the dispenser operation in the track printing system.

A mathematical model that allows describing the pastes extrusion has been selected. The numerical modeling has allowed obtaining a set of the parameters of the printing system making the system operation stable. The dependences of the volume fraction of the silver powder on the distance up to the dispenser vertical axis in the steady-state extrusion mode have been obtained. The dependence of the overpressure present on the vertical dispenser axis on the nozzle section distance at the outlet has been studied. The dependences of the maximum over-pressure present in the piston on its speed and the effective width of the track on the piston speed have been determined. The numerical modeling has shown that the paste viscosity influences significantly the extrusion process. An increase in the extrusion speed is shown to increase non-linearly the printed track width. Based on the mathematical model used in the work, a process for manufacturing prototypes of printed circuit boards with subsequent sintering will be developed.

#### Conflict of interest statement

The authors declare that they have no conflict of interest in relation to this research, whether financial, personal, authorship or otherwise, that could affect the research and its results presented in this paper.

#### CRedit author statement

Gadirov R.: Writing - Review & Editing, Conceptualization; Borisov A.: Methodology, Formal analysis; Trufanova N.: Writing - Original Draft; Ragimov E.: Visualization; Artischev S.: Supervision, Funding acquisition  
The final manuscript was read and approved by all authors.

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